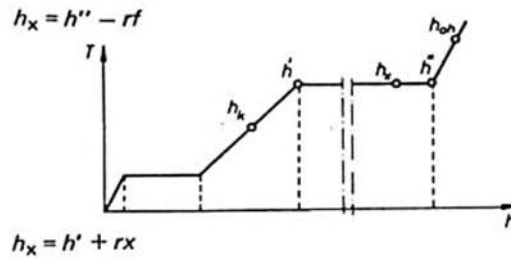


STEAM

Enthalpy



$$h_{oh} = h'' + c_{oh} \Delta T$$

Specific heat capacity
for superheated steam

$$c_{oh} = \frac{\Delta h_{oh}}{\Delta T_{oh}}$$

Steam density

$$\rho = \frac{1}{v}$$

Specific volume of
wet steam

$$v_x = v' (1 - x) + v'' x$$

h_x specific enthalpy
for wet steam J/kg
 h'' specific enthalpy for
dry saturated steam J/kg
 r evaporation heat J/kg
 f humidity 1

h' specific enthalpy
for boiling water J/kg
 x dryness 1

h_{oh} specific enthalpy for
superheated vapor J/kg
 c_{oh} specific heat
capacity for super-
heated vapor/steam J/kg · K
 ΔT temperature
difference K

Δh_{oh} enthalpy increase J/kg
 ΔT_{oh} temperature
increase K

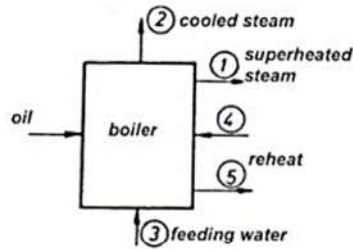
ρ density kg/m³
 v specific volume m³/kg

v_x specific volume of
wet steam m³/kg
 v' water volume m³/kg
 x dryness 1
 v'' steam volume m³/kg

Efficiency

Boiler efficiency

$$\eta_k = \frac{\dot{m}_1 h_1 + \dot{m}_2 h_2 + \dot{m}_5 h_5 - \dot{m}_3 h_3 - \dot{m}_4 h_4}{\dot{m}_B h_g}$$



η_k	boiler efficiency	1
\dot{m}_1	flow of superheated steam	kg/s
h_1	enthalpy of superheated steam	J/kg
\dot{m}_2	flow of cooled steam	kg/s
h_2	enthalpy of cooled steam	J/kg
\dot{m}_3	flow of feeder water	kg/s
h_3	enthalpy of feeder water	J/kg
\dot{m}_4	flow of reheated steam	kg/s
h_4	enthalpy in reheated steam to the boiler	J/kg
\dot{m}_5	flow of reheated steam	kg/s
h_5	enthalpy in reheated steam from the boiler	J/kg
\dot{m}_B	fuel consumption	kg/s
h_g	gross calorific value	J/kg

Turbine inner efficiency

$$\eta_i = \frac{H_i}{H_A} = \frac{h_{oh} - h_2}{h_{oh} - h_1}$$

η_i	inner efficiency of turbine	1
H_i	indicated decreased enthalpy	J/kg
H_A	adiabatic enthalpy fall	J/kg
h_{oh}	superheated steam enthalpy	J/kg
h_2	enthalpy of steam at real end condition, before condenser	J/kg
h_1	enthalpy of steam after adiabatic expansion	J/kg

Mechanical efficiency

$$\eta_m = \frac{P_s}{P_i}$$

η_m	mechanical efficiency	1
P_s	shaft effect	W
P_i	indicated effect	W

Thermo efficiency of turbine and condenser (without drain off and pre-heating)

$$\eta_{tp} = \frac{h_{oh} - h_2}{h_{oh} - h_k}$$

η_{tp} thermo efficiency of the process 1
 h_2 enthalpy at leaving turbine J/kg
 h_k enthalpy of condensate J/kg

Thermo efficiency of plant (without drain off and pre-heating)

$$\eta_{ta} = \frac{\dot{m}_D (h_{oh} - h_2)}{\dot{m}_B h_g} = \eta_{tp} \eta_k$$

η_{ta} thermo efficiency of the plant 1
 \dot{m}_D steam production kg/s
 η_k boiler efficiency 1

Flow in narrow pipes

$$c_o = \sqrt{2 (h_1 - h_2) + c^2}$$

c_o theoretic flow velocity m/s
 c velocity before "narrow pipe" m/s
 h_1 specific enthalpy (before) J/kg
 h_2 specific enthalpy (after) J/kg

$$c_o = 44.72 \sqrt{(h_1 - h_2)}$$

h_1 and h_2 are in kJ/kg

$$c_1 = c_o \phi$$

c_1 real flow velocity m/s
 ϕ velocity factor 1

Critical pressure

$$P_c = 0.577 p_1$$

p_c critical pressure Pa
 p_1 pressure before "narrow pipe" Pa

$$P_c = 0.546 p_1$$

0.577 factor for saturated steam
 0.546 factor for superheated steam

Steam flow

$$\dot{m}_D = \frac{A_c c_k}{v}$$

\dot{m}_D flow of steam kg/s
 A_c critical cross section (area) m²
 c_k critical velocity m/s
 v specific volume m³/kg

WORK OF STEAM (STEAM ENERGY)

Turbine without loss $W = \frac{1}{2} mc^2$

work J
 m mass kg
 c velocity m/s

$$W_n = \frac{1}{2} m (c_0^2 - c_1^2)$$

W_n loss at narrow Pipe J
 c_0 theoretic velocity m/s
 c_1 real velocity m/s

$$W_v = \frac{1}{2} m (\omega_1^2 - \omega_2^2)$$

W_v blade/vane loss J
 ω_1 relative in-velocity of steam m/s
 ω_2 relative out-velocity of steam m/s

$$W_\sigma = \frac{1}{2} m c_2^2$$

W_σ discharge flow (outward flow loss) J
 c_2 velocity from blades (vanes) m/s

Real turbine

$$W_e = W - W_n - W_v - W_\sigma$$

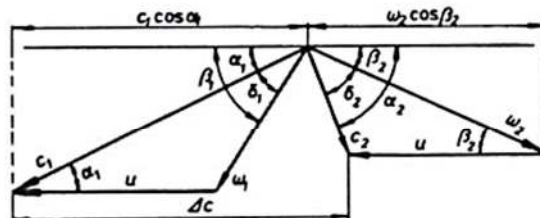
W_e real work J

$$W_e = \frac{1}{2} m [c_0^2 - (c_0^2 - c_1^2) - (\omega_1^2 - \omega_2^2) - c_2^2]$$

Trigonometric calculations of velocities

$$\omega_1^2 = c_1^2 + u^2 - 2c_1u \cos \alpha_1$$

ω_1 relative in-velocity of steam m/s
 c_1 velocity into narrow pipes m/s
 u rotation velocity of vanes m/s
 α_1 angle of "narrow pipe" rad



$$\frac{\sin \delta_1}{u} = \frac{\sin \alpha_1}{\omega_1}$$

$$\angle \beta_1 = \angle \alpha_1 + \angle \delta_1$$

β_1 in-angle of vanes rad

$$c_2^2 - \omega_2^2 + u^2 - 2\omega_2 u \cos \beta_2$$

c_2 absolute velocity outward from vanes m/s
 ω_2 relative out-velocity of steam m/s
 β_2 out-angle of vanes rad

$$\frac{\sin \delta_2}{u} = \frac{\sin \beta_2}{c_2}$$

$$\angle \alpha_2 = \angle \delta_2 + \angle \beta_2$$

α_2 out-angle of steam-jet rad

$$\Delta c = c_1 \cos \alpha_1 + \omega_2 \cos \beta_2 - u$$

Δc change of velocity m/s

$$\Delta c = \omega_1 \cos \beta_1 + \omega_2 \cos \beta_2$$

Effect

$$P = \dot{m}_0 u \Delta c$$

P effect W
 \dot{m}_0 steam flow kg/s

Degree of reaction

$$\rho = \frac{(\omega_2^2 - \omega_1^2)}{(c_1^2 - c_2^2) + (\omega_2^2 - \omega_1^2)}$$

ρ degree of reaction 1

Twisted blades/vanes

$$\delta = \beta'_1 - \beta_1$$

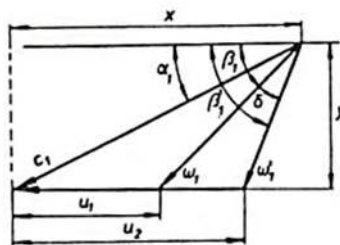
δ angular twist rad
 β'_1 in-angle of steam at end of vanes m/s
 β_1 in-angle of steam at root of vanes m/s

$$r_g \beta_1 = \frac{y}{x - u_1}$$

u_1 peripheral velocity at root m/s

$$r_g \beta'_1 = \frac{y}{x - u_2}$$

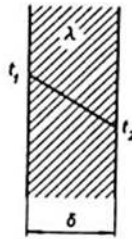
u_2 peripheral velocity at end m/s



ω_1 relative-velocity of steam at vane root m/s
 ω'_1 relative-velocity of steam at vane end m/s
 c^1 in-velocity of steam m/s
 α_1 in-angle of steam-jet rad

HEAT TRANSFER IN BOILERS

Heat conduction $P = \frac{\lambda}{\delta} A (T_1 - T_2)$



P	effect	W
λ	thermal conductivity	$W/m \cdot K$
δ	thickness of material	m
A	area	m^2
$T_1 - T_2$	temperature difference	K

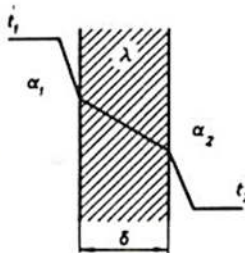
Convection $P = \alpha A (T_1 - T_2)$

P	effect	W
α	heat transfer coefficient	$W/m^2 \cdot K$

Simultaneous conduction and convection

$P = k A (T_1 - T_2)$

$$k = \frac{1}{\frac{1}{\alpha_1} + \frac{\delta}{\lambda} + \frac{1}{\alpha_2}}$$



P	effect	W
k	heat transfer (through) coefficient	$W/m^2 \cdot K$
α_1	heat transition coefficient gas - wall/material	W/m^2
α_2	heat transition coefficient water - wall/material	W/m^2
λ	thermal conductivity	$W/m \cdot K$
δ	thickness of material	m